# Theoretical background and application of MANSIM for ship maneuvering simulations

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#### Abstract

In this study, a new developed code, MANSIM (MANeuvering SIMulation) for ship maneuvering simulations and its theoretical background were introduced. In order to investigate the maneuverability of any low-speed ship with single-rudder/single-propeller (SPSR) or twin-rudder/twinpropeller (TPTR) configurations, a 3-DOF modular mathematical model or empirical approaches can be utilized in MANSIM. Not only certain maneuvers of ships such as, turning or zigzag but also free maneuver with unlimited number of rudder deflections can be simulated. Input parameters required to solve the equations of motion can be estimated practically by several empirical formulas that are embedded in the software. Graphical user interface of the code was designed simply so that users can perform maneuvering calculations easily. Besides displaying the results such as advance, transfer, tactical diameters etc. on the user interface, simulation results can also be analyzed graphically; thus it is possible to examine the variation of kinematic parameters during simulation. Using the code, maneuverabilities of a tanker ship (KVLCC2) and a surface combatant (DTMB5415) have been investigated and computed results were compared with free running data for validation. It is considered that MANSIM is quite advantageous for parametric studies and it is a valuable tool especially for sensitivity analysis on ship maneuvering. In this context, the effects of variation of hydrodynamic derivatives and rudder parameters on general maneuvering performance of ships were investigated by performing sensitivity analyses. It was found out that linear moment derivatives and rudder parameters are highly effective in maneuvering motion. Another interesting outcome of this study is the identification of the significance of third order coupled derivatives for DTMB5415 hull.

**Keywords:** hydrodynamic derivatives; DTMB5415; KVLCC2; MMG; sensitivity analysis; hull-rudder interaction

### Abbreviations

Ad	Advance	SB	System-Based
CFDB	CFD-Based	SDA	Steady Drift Angle
EMP	Empirical	SPSR	Single Propeller-Single Rudder
FR	Free Running	STD	Steady Turning Diameter
GUI	Graphical User Interface	STS	Steady Turning Speed
LCG	Longitudinal Center of Gravity	SYR	Steady Yaw Rate
MMG	Maneuvering Modelling Group	TD	Tactical Diameter
NR	Number of Rudders	TPTR	Twin Propeller-Twin Rudder
OA	Overshoot Angle	Tr	Transfer
Symbols A <sub>B</sub>	Submerged bow profile area	$T_P$	Thrust of propeller $(N)$
а <sub>н</sub>	$(m^2)$ Rudder lateral force increase factor (–)	u, v	Velocities in x and y axis at midship $(m/s)$
$A_R$	Profile area of movable part of mariner rudder $(m^2)$	$u_P$	Longitudinal inflow velocity to propeller $(m/s)$
В	Ship breadth $(m)$	$u_R, v_R$	velocity components to rudder, respectively $(m/s)$
$C_B$	Block coefficient $(-)$	U	Ship velocity at midship, $U = \sqrt{u^2 + v^2} (m/s)$
С	Rudder chord length $(m)$	$V_A$	Initial speed of ship (knots)
d	Ship mean draught $(m)$	$V_T$	Steady turning speed (knots)
$D_P$	Propeller diameter $(m)$	W <sub>P0</sub>	Effective wake fraction at propeller position in straight motion (–)
$f_{\alpha}$	Rudder lift gradient coefficient (–)	W <sub>P</sub>	Effective wake fraction at propeller position in maneuvering motion $(-)$

 $\mathbf{x}'_H$ 

 $\mathbf{x}_P', \mathbf{y}_P'$ 

 $\mathbf{x}_R', \mathbf{y}_R'$ 

 $X_H$ 

 $F_N$  Rudder normal force (N)

Fr Froude number (–)

H Rudder span (m)

g Gravity,  $g = 9.81 \ (m/s^2)$ 

(-)
Surge force due to hull in x axis
(N)

rudder position, respectively

Non-dimensional longitudinal

position of acting point of

additional lateral force (-) Non-dimensional longitudinal

and lateral position of propeller from midship (--) Non-dimensional longitudinal and lateral coordinate of

Iz	Yaw moment of inertia around z axis ( $kg m^2$ )	$X_R$	Surge force due to rudder in x axis (N)
Jz	Added yaw moment of inertia around z axis ( $kg m^2$ )	$X_P$	Surge force due to propeller in x axis $(N)$
$J_P$	Propeller advance ratio $(-)$	$Y_H$	Sway force due to hull in y axis ( <i>N</i> )
$k_0, k_1, k_2$	Propeller open water characteristics for expressing $K_T$ (-)	Y <sub>R</sub>	Sway force due to rudder in y axis $(N)$
K <sub>T</sub>	Thrust coefficient $(-)$	$\alpha_R$	Effective inflow angle to rudder ( <i>rad</i> )
$l'_R$	Flow-straightening coefficient of yaw rate for rudder, $l'_R = l_R/L$ (-)	$eta_P$	Geometrical inflow angle to propeller in maneuvering $(-)$
L	Overall length of ship $(m)$	$\beta_R$	Effective drift angle at rudder position ( <i>rad</i> )
т	Ship mass $(kg; t)$	β	Ship drift angle $(rad)$
$m_x$ , $m_y$	Added mass due to ship motion in x and y directions, respectively $(kg)$	$\gamma_R$	Flow-straightening coefficient of sway velocity for rudder $(-)$
$n_P$	Propeller revolution $(1/s)$	δ	Rudder angle $(rad)$
N <sub>H</sub>	Yaw moment due to hull around z axis $(N m)$	ε	Ratio of effective wake fraction in way of propeller and rudder (–)
N <sub>R</sub>	Yaw moment due to rudder around z axis $(N m)$	η	Ratio of propeller diameter to rudder span (–)
$o_0 - x_0 y_0 z_0$	Earth-fixed coordinate system	κ	An experimental constant for expressing $u_R(-)$
o - xyz	Ship-fixed coordinate system	Λ	Rudder aspect ratio $(-)$
r	Yaw rate around z axis at midship $(rad/s)$	ρ	Water density $(kg/m^3)$
S	Wetted surface area of ship $(m^2)$	τ	Static Trim $(m)$
$t_P$	Propeller thrust deduction factor in maneuvering motions (-)	$\psi$	Ship heading angle $(rad)$
$t_R$	Steering resistance deduction factor (–)		

# 1 Introduction

Prediction of maneuverability of ships is one of the most challenging topics in ship hydrodynamics. Maneuvering simulations are generally carried out by using CFD-based or system-based (SB) methods. CFD-based method can be defined as a direct simulation of the actual maneuvering motion, including the steering rudder and rotating propeller (Bhushan et al., 2009; Carrica et al., 2013; Broglia et al., 2015; Ohashi et al., 2018; Duman and Bal, 2019). From practical point of view, this approach is not feasible as it requires enourmous computational power to perform full time-domain simulations. On the other hand, SB methods include the solution of equations of motion for every time step using the

previously calculated hydrodynamic derivatives. The latter method is much more practical than the former one, however it's accuracy directly depends on the selected mathematical model and the hydrodynamic derivatives involved (Guo and Zou, 2017; Toxopeus et al., 2018; Sukas et al., 2019). In the recent literature, current trend to express the hydrodynamic forces and moments is to use either Abkowitz model (Abkowitz, 1964) or MMG model (Ogawa and Kasai, 1978; Yoshimura, 2005; Yasukawa and Yoshimura, 2015). In Abkowitz model; hull, rudder and propeller are considered as one rigid body, and equations of motion are defined by using a function based on third-order Taylor series. Unlike Abkowitz model, MMG model is a simplified mathematical model that decomposes total hydrodynamic force and moment acting on the ship into hull, rudder and propeller components. One of the biggest advantages of MMG model is that it allows to take the hull-rudder-propeller interactions into account. Many results of maneuvering simulations have been presented so far using MMG model with different modified versions (Fang et al., 2005; Kang et al., 2008; He et al., 2016; Yasukawa et al., 2019).

There are several prediction methods proposed in literature to determine the hydrodynamic derivatives in MMG models (Sukas et al., 2017a; Sukas et al., 2017b). For example, Yasukawa and Yoshimura (2015) carried out circular motion tests (CMT) to obtain the hydrodynamic derivatives and it was noted that CMT is a suitable method since it has a zero frequency of motion which reduces the uncertainties for hydrodynamic forces and moment. PMM (Planar Motion Mechanism) tests are also widely used to determine the hydrodynamic derivatives (Cura-Hochbaum, 2011; Obreja et al. 2012; Sakamoto et al., 2012; Yoon et al., 2015; Duman and Bal, 2017). Accuracy of results based on the selection of PMM motion frequency and amplitude may even change, however this issue can be handled if PMM motion parameters are selected properly according to ITTC Recommendations (ITTC 7.5-02-06-02, 2014). A recent study has shown that changing the advancing speed of ship in PMM tests has a significant effect on the hydrodynamic derivatives in MMG model (Zhang et al., 2019). In addition to these methods, Liu et al. (2017) presented an integrated empirical maneuvering model for inland vessels and all hydrodynamic derivatives and propeller/rudder parameters in MMG model were estimated by various regression formulas from literature. On the other hand, system identification techniques have been also used for estimation of hydrodynamic derivatives (Zhang and Zou, 2013; Sutulo and Soares, 2014; Yin et al., 2015; Xu et al., 2019). In order to predict maneuverability of any ship using system-based approach, these methods can be utilized to obtain the hydrodynamic derivatives, propeller/rudder parameters.

In this study, a new user-friendly ship maneuvering code called MANSIM (MANeuvering SIMulation) that is based on standard MMG mathematical model (Yasukawa and Yoshimura, 2015), is introduced. The code includes several empirical relations suggested by various researchers working on the topic and is for those who would like to have a fundamental background of the maneuvering abilities a ship during early design stages. The primary aim here by developing such a code is to make the maneuvering predictions of ships easier by using a simple user interface. The software allows to simulate the turning and zigzag maneuvers of ships. In addition, a free maneuvering results such as advance distance, transfer distance, tactical diameter etc. Input parameters of the mathematical model, such as hydrodynamic derivatives and coefficients related to the propeller and rudder, can also be estimated by several empirical formulas embedded in the software. The empirical approach provided by Lyster and Knights (1978) may also be preferred as a second option to have a basic understanding of maneuvering abilities of a ship.

Following this section, section 2 presents the theoretical background of MANSIM including the empirical approach suggested by Lyster and Knights (1978) and MMG models for SPSR and TPTR ships. Section 3 gives the empirical formulas embedded in software to estimate input parameters of MMG model. The GUI of code was briefly introduced and sample screenshots were given in Section 4. In section 5, maneuverability of two benchmark ships (KVLCC2 and DTMB5415) was examined for validation purposes and the results predicted were compared with the free running test data. In addition, the effect of variation of hydrodynamic derivatives and rudder parameters on general maneuvering performance was investigated by performing a parametrical sensitivity analysis. Finally, a brief conclusion of the study was drawn and future studies about MANSIM were mentioned in section 6.

# 2 Theoretical Background

In MANSIM, maneuvering performance of ships can be predicted using either the empirical model provided by Lyster and Knights (1979) and the mathematical models presented by Khanfir et al. (2011) and Yasukawa and Yoshimura (2015). Further details are explained in the following sub-sections.

# 2.1 Empirical Approach

Range (maximum and minimum values) of parameters for ships used in the study of Lyster and Knights (1979) are given in Table 1. The empirical formulations have been derived based on the model experiments.

	Single – Propeller Ships		Twin – Propeller Ships	
Parameters	Min.	Max.	Min.	Max.
$L_{PP}[m]$	54.86	329.18	76.20	225.55
$C_B$	0.56	0.87	0.42	0.62
$\delta$	10.00	45.00	10.00	35.00
B/L	0.11	0.18	0.06	0.20
$\tau/L$	0.00	0.05	-0.01	0.03
Hc/Ld	0.01	0.04	0.01	0.02
$V_A/\sqrt{L}$	0.20	1.00	0.25	2.20

Table 1. Range of ship parameters used in the study of Lyster and Knights (1979).

Turning maneuver indices of SPSR ships can be calculated by the following semi-empirical expressions:

$$\frac{\text{STD}}{\text{L}} = 4.19 - 203 \frac{\text{C}_{\text{B}}}{\delta} - 13.0 \frac{\text{B}}{\text{L}} + \frac{194}{\delta} - 35.8 \frac{\text{Hc}}{\text{Ld}}(\text{ST} - 1) + 3.82 \frac{\text{Hc}}{\text{Ld}}(\text{ST} - 2) + 7.79 \frac{\text{A}_{\text{B}}}{\text{Ld}}$$
(1)

$$\frac{\text{TD}}{\text{L}} = 0.910 \frac{\text{STD}}{\text{L}} + 0.424 \frac{V_A}{\sqrt{L}} + 0.675$$
(2)

$$\frac{Ad}{L} = 0.519 \frac{TD}{L} + 1.33$$
(3)

$$\frac{\text{Tr}}{\text{L}} = 0.497 \frac{\text{TD}}{\text{L}} - 0.065$$
(4)  
$$\frac{\text{V}_{\text{T}}}{\text{V}_{\text{A}}} = 0.074 \frac{\text{TD}}{\text{L}} + 0.149$$
(5)

where,

#### ST = 1 if $dc \le Hc$ , ST = 2 if dc > Hc

For TPTR ships, the empirical formulas for turning maneuver indices are given as follows:

$$\frac{\text{STD}}{\text{L}} = 0.727 - 197 \frac{\text{C}_{\text{B}}}{\delta} + 4.65 \frac{\text{B}}{\text{L}} + \frac{188}{\delta} - 218 \frac{\text{Hc}}{\text{Ld}} (\text{NR} - 1) + 1.767 \frac{\text{V}_{\text{A}}}{\sqrt{\text{L}}} + 25.56 \frac{\text{A}_{\text{B}}}{\text{Ld}}$$
(6)

$$\frac{\text{TD}}{\text{L}} = \frac{\text{STD}}{\text{L}} + 0.14 \tag{7}$$

$$\frac{Ad}{L} = 0.514 \frac{TD}{L} + 1.1 \tag{8}$$

$$\frac{\text{Tr}}{\text{L}} = 0.531 \frac{\text{TD}}{\text{L}} - 0.357 \tag{9}$$

$$\frac{V_{\rm T}}{V_{\rm A}} = 0.028 \frac{\rm TD}{\rm L} + 0.543 \tag{10}$$

Here, Ad, Tr, TD, STD and  $V_T$  represent the turning maneuver indices and are called advance, transfer, turning diameter, steady turning diameter and steady turning speed, respectively. L, B, d and  $C_B$  are the main particulars of ship.  $A_B$  is the area of submerged bow profile,  $\tau$  is the static trim and  $V_A$  is the initial approach velocity of ship. Parameters related to rudder are rudder angle ( $\delta$ ), span length (H), chord length (c) and number of rudders (NR).

#### 2.2 Modular Mathematical Model

In the MMG model, hydrodynamic forces and moment acting on the ship are broken into different parts (contributors) such as hull, rudder(s) and propeller(s). The major advantage of this method compared to traditional approach (Abkowitz-type) is the inclusion of interaction effects of hull-rudder(s) and hull-propeller(s). Some assumptions in MANSIM have been done, due to the implementation of MMG model (Yasukawa and Yoshimura, 2015). They are given below.

- Hydrodynamic forces and moment acting on the ship treat quasi-steadily.
- Cruise speed of the ship is sufficiently low so that wave-making resistance is ignored.
- Metacentric height (GM) is quite large, thus effects of roll-coupling are negligible.

In the present version of MANSIM, mathematical models for SPSR (Yasukawa and Yoshimura, 2015) and TPTR (Khanfir et al., 2011) ships are available to predict the maneuvering performance in calm water condition. Following sections present the coordinate system, non-dimensionalization and the mathematical models for SPSR and TPTR ships, respectively.

### 2.2.1 Coordinate System and Non-Dimensionalization

The basic dynamic of motion is described using the Newton's second law of motion, thus two different coordinate systems can be defined for a maneuvering ship: earth-fixed coordinate system ( $O - X_0Y_0Z_0$ ) and ship-fixed (o - xyz) coordinate system as shown in Figure 1.



Figure 1. Coordinate system used in calm water.

Here heading angle  $\psi$  refers to angle between x and  $x_0$  axis. The difference between ship's heading and actual course direction (velocity vector at COG) is drift angle,  $\beta = \tan^{-1}(-v/u)$ . The rudder angle,  $\delta$  is positive while rotating to starboard side. u and v denote velocity components in x and y directions, respectively. r is the yaw rate that can also be defined as  $r = \frac{\partial \psi}{\partial t}$ . The speed of ship is indicated as  $U (= \sqrt{u^2 + (-v)^2})$ .

In MANSIM, hydrodynamic forces and moment, mass, added mass, moment of inertia, added moment of inertia and other kinematical parameters are non-dimensionalized as given in Table 2.

Parameters	Non-dimensionalized by
Х, Ү	$\frac{1}{2}\rho U^2 Ld$
Ν	$\frac{1}{2}\rho U^2 L^2 d$
<i>u</i> , <i>v</i>	U
r	U/L
$m, m_x, m_y$	$\frac{1}{2}\rho L^2 d$

Table 2. Non-dimensionalization of ship and kinematical parameters.

#### 2.2.2 Mathematical Model

Maneuverability of only low-speed ships in the horizontal plane with sufficiently large GM is considered in the mathematical model of MANSIM. Ship motions in six degree-of-freedom (6-DOF) reduce to 3-DOF under the following assumptions:

- Vertical motions (heave, pitch and roll) are ignored. Then  $w = p = q = \dot{w} = \dot{p} = \dot{q} = 0$ .
- It is assumed that the ship has symmetry over xz plane, then  $y_G = 0$ .

In this case, 3-DOF motion equations become:

$$m[\dot{u} - rv - x_G r^2] = F_x$$

$$m[\dot{v} + ur + x_G \dot{r}] = F_y$$

$$I_{zG}\dot{r} + mx_G(\dot{v} + ur) = N_z$$
(11)

Forces and moments on the right hand sides of these equations can be written separately:

$$F_x = -m_x \dot{u} + m_y vr + X$$

$$F_y = -m_y \dot{v} - m_x ur + Y$$

$$N_z = -J_z \dot{r} + N - x_G F_y$$
(12)

3-DOF motion equations then become;

$$(m + m_{x})\dot{u} - (m + m_{y})vr - x_{G}mr^{2} = X$$

$$(m + m_{y})\dot{v} + (m + m_{x})ur + x_{G}m\dot{r} = Y$$

$$(I_{zG} + x_{G}^{2}m + J_{z})\dot{r} + x_{G}m(\dot{v} + ur) = N$$
(13)

X, Y and N can be divided into its components due to the modular structure of MMG model:

$$X = X_H + X_R + X_P$$

$$Y = Y_H + Y_R$$

$$N = N_H + N_R$$
(14)

where the subscripts H, R and P refer to hull, rudder and propeller, respectively. 3-DOF motion equations can be written in matrix form as follows,

$$Acc = M^{-1} \cdot (P - C \cdot Vel) \tag{15}$$

where Acc matrix includes acceleration terms ( $Acc = [\dot{u} \quad \dot{v} \quad \dot{r}]^T$ ), P forces and moments ( $P = [X_H + X_R + X_P \quad Y_H + Y_R \quad N_H + N_R]^T$ ) and Vel the velocity terms ( $Vel = [u \quad v \quad r]^T$ ).  $M^{-1}$  is the inverse of mass matrix and C is the Coriolis matrix. Mass matrix M and Coriolis matrix C are given as follows:

$$M = \begin{bmatrix} m + m_x & 0 & 0 \\ 0 & m + m_y & x_G m \\ 0 & x_G m & I_{ZG} + x_G^2 m + J_Z \end{bmatrix}$$
(16a)

$$C = \begin{bmatrix} 0 & -(m+m_y)r & -x_G mr \\ (m+m_x)r & 0 & 0 \\ x_G mr & 0 & 0 \end{bmatrix}$$
(16b)

Using all these matrices, Eqn.15 can be written explicitly as;

$$\begin{bmatrix} \dot{u} \\ \dot{v} \\ \dot{r} \end{bmatrix} = \begin{bmatrix} 1/M_{11} & 0 & 0 \\ 0 & M_{33}/\det M & -M_{32}/\det M \\ 0 & -M_{23}/\det M & M_{22}/\det M \end{bmatrix} \cdot \begin{bmatrix} X_H + X_R + X_P + v(m + m_y) + rx_G mr \\ Y_H + Y_R - (m + m_x)ur \\ N_H + N_R - x_G mur \end{bmatrix}$$
(17)

The first equation is solved separately, while the others need to have a coupled solution. The moment of inertia around z axis in the mass matrix M is not given by the user, but assumed as approximately  $I_z \cong m(0.25L_{pp})^2$ . External forces and moment given in the right-hand side (RHS) of Eqn.13 are explained in the following sub-sections.

#### 2.2.2.1 Hull Forces and Moment

Hydrodynamic forces and moment acting on both SPSR and TPTR hulls are expressed as follows (Yasukawa and Yoshimura, 2015):

$$X_{H} = -X_{0}(u) + X_{vv}v^{2} + X_{vr}vr + X_{rr}r^{2} + X_{vvvv}v^{4}$$

$$Y_{H} = Y_{v}v + Y_{r}r + Y_{vvv}v^{3} + Y_{vvr}v^{2}r + Y_{vrr}vr^{2} + Y_{rrr}r^{3}$$

$$N_{H} = N_{v}v + N_{r}r + N_{vvv}v^{3} + N_{vvr}v^{2}r + N_{vrr}vr^{2} + N_{rrr}r^{3}$$
(18)

where all coefficients here ( $X_{vv}$ ,  $Y_{vvv}$ ,  $Y_{vrr}$ ,  $N_{rrr}$ , etc.) are known as hydrodynamic derivatives or maneuvering coefficients.

#### 2.2.2.2 Propeller Forces and Moment

Propeller surge force  $(X_P)$  is calculated for SPSR (Yasukawa and Yoshimura, 2015) and TPTR (Khanfir et al., 2011) ships with the parameters given in Table 3. Note that side force  $(Y_P)$  and yaw moment  $(N_P)$  due to propeller are neglected as they have smaller magnitudes compared to those of hull and rudder components. The superscripts 'P' and 'S' in Table 3 represent port and starboard propellers, respectively.

Table 3. Hydrody	ynamic force du	e to pro	peller for sir	ngle and twin	propeller ships
				0	

Definition	Single-Propeller Ships	Twin-Propeller Ships
Surge force due to propeller(s)	$X_P = (1 - t_P)T_p$	$X_{P}^{P,S} = (1 - t_{P}^{P,S})T_{p}^{P,S}$
Thrust of propeller(s)	$T_p = \rho n_P^2 D_P^4 K_T$	$T_p^{P,S} = \rho n_P^2 D_P^4 K_T^{P,S}$
Thrust coefficent	$K_T = k_0 + k_1 J_P + k_2 J_P^2$	$K_T^{P,S} = k_0 + k_1 J_P^{P,S} + k_2 (J_P^{P,S})^2$
Propeller(s) advance ratio	$J_P = \frac{u_P}{n_P D_P}$	$J_P^{P,S} = \frac{u_P^{P,S}}{n_P D_P^{P,S}}$
Inflow velocity to propeller(s)	$u_P = u(1-w_P)$	$u_P^{P,S} = (1 - w_P^{P,S})(u + y_P^{P,S}r)$
Wake fraction of propeller(s)	$w_P = w_{P0} \exp(-4\beta_P^2)$	$w_P^{P,S} = w_{P0}^{P,S} \exp(-4(\beta_P^{P,S})^2)$
Geometrical inflow angle	$eta_P=eta-\mathrm{x}_P'r'$	$\beta_P^{P,S} = \beta - (\mathbf{x}_P')^{P,S} r'$

Here,  $t_P$  is propeller thrust deduction factor in maneuvering motion,  $n_P$  is propeller rotation rate and  $D_P$  is propeller diameter.  $k_0$ ,  $k_1$  and  $k_2$  represent open water characteristics of propeller for expressing  $K_T$ .  $w_{P0}$  denotes the effective wake fraction at propeller position in straight motion and  $x'_P$  is nondimensional longitudinal position of propeller from midship.

#### 2.2.2.3 Rudder Forces and Moment

Forces and moment related to rudder  $(X_R, Y_R, N_R)$  for single-rudder ships are calculated based on rudder normal force  $(F_N)$ , rudder angle  $(\delta)$  and hull-rudder interaction coefficients  $(t_R, a_H, x_H)$  by the following equations (Yasukawa and Yoshimura, 2015):

$$X_{R} = -(1 - t_{R})F_{N}\sin\delta$$

$$Y_{R} = -(1 + a_{H})F_{N}\cos\delta$$

$$N_{R} = -(x_{R} + a_{H}x'_{H})F_{N}\cos\delta$$
(19)

where  $t_R$  is steering resistance deduction factor.  $a_H$  and  $x'_H$  are rudder lateral force increase factor and non-dimensional longitudinal position of acting point of  $a_H$  from midship, respectively. For twin rudder ships, hydrodynamic forces and moment due to rudders are calculated by (Khanfir et al., 2011):

$$X_{R} = -(1 - t_{R})(F_{N}^{P}sin\delta^{P} + F_{N}^{S}sin\delta^{S})$$

$$Y_{R} = -(1 + a_{H})(F_{N}^{P}cos\delta^{P} + F_{N}^{S}cos\delta^{S})$$

$$N_{R} = -(x_{R} + a_{H}x'_{H})(F_{N}^{P}cos\delta^{P} + F_{N}^{S}cos\delta^{S}) + (1 - t_{R})(y_{R}^{P}F_{N}^{P}sin\delta^{P} + y_{R}^{S}F_{N}^{S}sin\delta^{S})$$
(20)

Here  $y_R^P$  and  $y_R^S$  are the offsets of rudders from the ship's centerline. Parameters required for prediction of rudder normal force(s) ( $F_N$ ) during maneuver are given in Table 4.

Definition	Single-Rudder Ships	Twin-Rudder Ships
Rudder normal	$F_N = 0.5 \rho A_R U_R^2 f_\alpha \sin \alpha_R$	$F_N^{P,S} = 0.5 \rho A_R^{P,S} (U_R^{P,S})^2 f_\alpha^{P,S} \sin \alpha_R^{P,S}$
force Buddor lift		
gradient	$f = \frac{6.13\Lambda}{1}$	$\epsilon^{P,S}$ – $6.13\Lambda^{P,S}$
coefficient	$J_{\alpha} = \Lambda + 2.25$	$J_{\alpha} = \frac{1}{\Lambda^{P,S} + 2.25}$
Inflow velocity	$U_{\rm p} = \sqrt{\mu^2 + \mu^2}$	$U^{P,S} = \sqrt{(u^{P,S})^2 + (u^{P,S})^2}$
to rudders	$\sigma_R = \sqrt{a_R + \sigma_R}$	$U_R = \sqrt{(u_R) + (v_R)}$
Effective inflow	$v_R$	$V_{p}^{P,S}$
angle to	$\alpha_R = \delta - \tan^{-1}(\frac{1}{u_R})$	$\alpha_R^{P,S} = \delta^{P,S} - (\gamma_R^{P,S} \beta_R^{P,S} - \tan^{-1}(\frac{\gamma_R}{\chi_P^{P,S}}))$
rudder(s)		жp
Effective inflow		
angle to	$\beta_P = \beta - l'_P r'$	$\beta_{P}^{P,S} = \beta - (l_{P}^{\prime})^{P,S} r^{\prime}$
rudder(s) in		
maneuvering		

Table 4. Rudder parameters required to calculate the rudder normal force(s).

Longitudinal inflow velocity to rudder(s)	$u_{R} = \varepsilon u_{P} \sqrt{\eta \left\{ 1 + \kappa \left( \sqrt{1 + \frac{8K_{T}}{\pi J_{P}^{2}} - 1} \right) \right\}^{2} + (1 - \eta)}$	$u_{R}^{P,S} = \varepsilon^{P,S} u_{P}^{P,S} \sqrt{\eta \left\{ 1 + \kappa^{P,S} \left( \sqrt{1 + \frac{8K_{T}^{P,S}}{\pi (J_{p}^{P,S})^{2}} - 1 \right) \right\}^{2} + (1 - \eta)}$
Lateral inflow velocity to rudder(s)	$ u_R = \gamma_R eta_R$	$v_R^{P,S} = u_R^{P,S} \tan(\gamma_R^{P,S} \beta_R^{P,S} - \tan^{-1}(\frac{y_R^{P,S}}{x_P^{P,S}}))$

Here,  $\varepsilon$ ,  $\kappa$ ,  $l_R$  and  $\gamma_R$  are the unknown rudder parameters that need to be estimated empirically, numerically or experimentally.  $A_R$  is the profile area of movable part of rudder,  $\Lambda$  is aspect ratio of rudder and  $\eta$  is ratio of propeller diameter to rudder span. Note that equation provided for rudder lift gradient coefficient ( $f_{\alpha}$ ) is suggested by Fujii and Tuda (1961).

# 3 Empirical Equations

All input parameters should be inserted to obtain full maneuvering performance of a ship in MANSIM. In case no input data is available for hydrodynamic parameters of hull, rudder and propeller; empirical relations embedded in MANSIM can be applied. These empirical equations are taken from various studies in literature. From practical point of view, empirical formulas may be useful to assess the order of magnitudes of parameters in the preliminary design stage. The empirical formulas embedded in MANSIM are given in the following sub-sections.

### 3.1 Added Mass and Added Moment of Inertia

The empirical formulas embedded in software for the estimation of added masses  $m_x$ ,  $m_y$  and added moment of inertia  $J_z$  are given in Table 5. All formulas provided are based on the main particulars of ship such as; m, L, B, d and  $C_B$ . It should be noted that  $m_x$  is advised to be taken approximately as %3 - 6 of ship mass (m) in Clarke et. al. (1983), where it is taken as %5 of ship mass in MANSIM.

-	
Reference	Empirical Formula
Clarke et. al. (1983)	$m_x = m * 0.05$
Zhou et. al. (1983)	$m_Y = m \left[ 0.882 - 0.54C_B \left( 1 - 1.6 \frac{d}{B} \right) - 0.156(1 - 0.673C_B) \frac{L}{B} + 0.826 \frac{d}{B} \frac{L}{B} \left( 1 - 0.678 \frac{d}{B} \right) - 0.638C_B \frac{d}{B} \frac{L}{B} \left( 1 - 0.669 \frac{d}{B} \right) \right]$
Zhou et. al. (1983)	$J_Z = m \left[ \frac{1}{100} \left( 33 - 76.85C_B (1 - 0.784C_B) + 3.43 \frac{L}{B} (1 - 0.63C_B) \right) \right]^2$

Table 5. En	npirical relation	ns to estimate	$m_{\rm r}, m_{\rm Y}$	and $I_z$
			· · · · · · · · · · · · · · · · · · ·	JZ.

### 3.2 Hydrodynamic Derivatives

In this section, the empirical formulas existed in the software to estimate the hydrodynamic derivatives are presented. Table 6, Table 7 and Table 8 show the empirical formulas provided for derivatives related to surge force (X), sway force (Y) and yaw moment (N), respectively. The total resistance coefficient ( $X'_0$ ) is calculated by Holtrop method (Holtrop, 1978). Note that the accuracy of empirical

relations may change with range of ship parameters and mathematical model used in the corresponding study. Note that all empirical equations given in Tables 6-8 have been rearranged according to the non-dimensionalization procedure used in MANSIM.

Reference	Empirical Formula
Lee et. al. (1998)	$X_{VV} = 0.0014 - 0.1975d \frac{(1 - C_B)L}{B} \frac{L}{d}$
Yoshimura and Masumoto (2012)	$X_{VV} = 1.15 \frac{C_B}{L/B} - 0.18$
Yoshimura and Masumoto (2012)	$X_{VVVV} = -6.68 \frac{C_B}{L/B} + 1.1$
Lee et. al. (1998)	$X_{rr} = \left(-0.0027 + 0.0076C_B \frac{d}{B}\right) \frac{L}{d}$
Yoshimura and Masumoto (2012)	$X_{rr} = -0.085 \frac{C_B}{L/B} + 0.008 - x_G m_y$
Lee et. al. (1998)	$X_{vr} = \left[m + 0.1176m_y(0.5 + C_B)\right] \frac{L}{d}$
Yoshimura and Masumoto (2012)	$X_{vr} = m_y - 1.91 \frac{C_B}{L/B} + 0.08$

**Table 6**. Empirical formulas for hydrodynamic derivatives for surge force (*X*).

**Table 7**. Empirical formulas for hydrodynamic derivatives for sway force (Y).

Reference	Empirical Formula
Kijima et. al. (1990)	$Y_{\nu} = -\left(0.5\pi \frac{2d}{L} + 1.4C_B \frac{B}{L}\right)$
Lee et. al. (1998)	$Y_{\nu} = \left(-0.4545 \frac{d}{L} + 0.065 C_B \frac{B}{L}\right) \frac{L}{d}$
Yoshimura and Masumoto (2012)	$Y_{\nu} = -\left(0.5\pi \frac{2d}{L} + 1.4 \frac{C_B}{L/B}\right)$
Clarke et. al. (1983)	$Y_{\nu} = \left[ -\pi \left( \frac{d}{L} \right)^2 \left( 1 + 0.4C_B \frac{B}{d} \right) \right] \frac{L}{d}$
Smitt (1970)	$Y_{\nu} = -\pi \left(\frac{d}{L}\right)^2 1.59 \ \frac{L}{d}$
Norrbin (1971)	$Y_{\nu} = \left[ -\pi \left( \frac{d}{L} \right)^2 \left( 1.69 + 0.08 \frac{C_B}{\pi} \frac{B}{d} \right) \right] \frac{L}{d}$
Inoue et. al. (1981)	$Y_{\nu} = \left[ -\pi \left( \frac{d}{L} \right)^2 \left( 1 + \frac{1.4}{\pi} C_B \frac{B}{d} \right) \right] \frac{L}{d}$
Khattab (1984)	$Y_{\nu} = \left[ -\pi \left(\frac{d}{L}\right)^2 \left(\frac{2.3}{\pi} + \frac{1.466}{\pi} C_B \frac{B}{d} - \frac{0.00102}{\pi} \left(\frac{L}{d}\right)^2 \right] \frac{L}{d}$
Ankudinov (1987)	$Y_{v} = \left[ -\pi \left(\frac{d}{L}\right)^{2} K_{y}(0.25(C_{B}\frac{B}{d})^{2} - 1.5C_{B}\frac{B}{d} + 3.45) \right] \frac{L}{d}$ if $C_{B}\frac{B}{d} > 5$ $K_{y} = 5\frac{d}{C_{B}B}$ ; else $K_{y} = 1$
Lee et. al. (1998)	$Y_{\nu\nu\nu} = \left(-0.6469(1 - C_B)\frac{d}{B} + 0.0027\right)\frac{L}{d}$

Yoshimura and Masumoto (2012)	$Y_{vvv} = -0.185 \frac{L}{B} + 0.48$
Kijima et. al. (1990)	$Y_r = (m + m_x) - 1.5C_B \frac{B}{L}$
Lee et. al. (1998)	$Y_r = \left(-0.115C_B \frac{B}{L} + 0.0024\right) \frac{L}{d}$
Yoshimura and Masumoto (2012)	$Y_r = m_x + 0.5C_B \frac{B}{L}$
Clarke et. al. (1983)	$Y_r = \left[ -\pi \left(\frac{d}{L}\right)^2 \left( -0.5 + 2.2 \frac{B}{L} - 0.080 \frac{B}{d} \right) \right] \frac{L}{d}$
Smitt (1970)	$Y_r = \left[-\pi \left(\frac{d}{L}\right)^2 \left(-0.32\right)\right] \frac{L}{d}$
Norrbin (1971)	$Y_r = \left[ -\pi \left(\frac{d}{L}\right)^2 \left( -0.645 + 0.38 \frac{C_B}{\pi} \frac{B}{d} \right) \right] \frac{L}{d}$
Inoue et. al. (1981)	$Y_r = \left[ (-0.5) \left( -\pi \left(\frac{d}{L}\right)^2 \right) \right] \frac{L}{d}$
Khattab (1984)	$Y_r = \left[ -\pi \left(\frac{d}{L}\right)^2 \left(\frac{-1.0328}{\pi} - \frac{0.11}{\pi} C_B \frac{B}{d} - \frac{0.00004}{\pi} \left(\frac{L}{d}\right)^2 \right] \frac{L}{d}$
Ankudinov (1987)	$Y_{r} = \left[ -\pi \left( \frac{d}{L} \right)^{2} \left( -\left( 0.3 - C_{B} \frac{B}{L} \right) Y_{v} \left( -\pi \left( \frac{d}{L} \right)^{2} \right) \right) \right] \frac{L}{d}$
Lee et. al. (1998)	$Y_{rrr} = \left[ -0.0233C_B \frac{d}{B} + 0.0063 \right] \frac{L}{d}$
Yoshimura and Masumoto (2012)	$Y_{rrr} = -0.051$
Kijima et. al. (1990)	$Y_{vrr} = -\left[5.95d \frac{(1-C_B)}{B}\right]$
Lee et. al. (1998)	$Y_{vrr} = -\left[0.4346(1-C_B)\frac{d}{B}\right]\frac{L}{d}$
Yoshimura and Masumoto (2012)	$Y_{vrr} = -\left[0.26(1 - C_B)\frac{L}{B} + 0.11\right]$
Kijima et. al. (1990)	$Y_{vvr} = 1.5d  \frac{C_B}{B} - 0.65$
Lee et. al. (1998)	$Y_{vvr} = \left(0.1234C_B \frac{d}{B} - 0.001452\right) \frac{L}{d}$
Yoshimura and Masumoto (2012)	$Y_{vvr} = -0.75$

# **Table 8**. Empirical formulas for hydrodynamic derivatives for yaw moment (N).

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Reference	Empirical Formula
Kijima et. al. (1990)	$N_{\nu} = -2\frac{d}{L}$
Lee et. al. (1998)	$N_{\nu} = (-0.23 \frac{d}{L} + 0.0059) \frac{L}{d}$

$$\begin{split} N_{v} &= -2\frac{d}{L} \\ N_{v} &= (-\pi \left(\frac{d}{L}\right)^{2} \left(0.5 + 2.4\frac{d}{L}\right))\frac{L}{d} \\ N_{v} &= (-\pi \left(\frac{d}{L}\right)^{2} \left(0.64 - 0.04\frac{C_{B}B}{\pi d}\right))\frac{L}{d} \\ N_{v} &= (-\pi \left(\frac{d}{L}\right)^{2} \left(0.64 - 0.04\frac{C_{B}B}{\pi d}\right))\frac{L}{d} \\ N_{v} &= \left(-\pi \left(\frac{d}{L}\right)^{2} \left(\frac{1.758}{\pi} - \frac{0.00768}{\pi d}\frac{C_{B}L^{2}}{Bd} - \frac{0.0008}{\pi} \left(\frac{L}{d}\right)^{2}\right)\right]\frac{L}{d} \\ N_{v} &= \left[-\pi \left(\frac{d}{L}\right)^{2} \left(0.75 - 0.04\frac{C_{B}B}{\pi d}\right)\right]\frac{L}{d} \\ N_{vvv} &= \left[-\pi \left(\frac{d}{L}\right)^{2} \left(0.75 - 0.04\frac{C_{B}B}{\pi d}\right)\right]\frac{L}{d} \\ N_{vvvv} &= \left[0.0348 - 0.5283(1 - C_{B})\frac{d}{B}\right]\frac{L}{d} \\ N_{vvvv} &= -\left[-0.69C_{B} + 0.66\right] \\ N_{r} &= -0.54\frac{2d}{L} + \left(\frac{2d}{L}\right)^{2} \\ N_{r} &= \left[-0.003724 + 0.10446\frac{d}{L} - 1.393\left(\frac{d}{L}\right)^{2}\right]\frac{L}{d} \\ N_{r} &= \left[-\pi \left(\frac{d}{L}\right)^{2} \left(0.25 + 0.039\frac{B}{d} - 0.56\frac{B}{L}\right)\right]\frac{L}{d} \\ N_{r} &= \left[-\pi \left(\frac{d}{L}\right)^{2} \left(0.47 - 0.18\frac{C_{B}B}{\pi d}\right)\right]\frac{L}{d} \\ N_{r} &= \left[-\pi \left(\frac{d}{L}\right)^{2} \left(0.47 - 0.18\frac{C_{B}B}{\pi d}\right)\right]\frac{L}{d} \\ N_{r} &= \left[-\pi \left(\frac{d}{L}\right)^{2} \left(\frac{1.3192}{\pi} - 0.68228\frac{C_{B}}{\pi} - \frac{0.00019}{\pi}\left(\frac{L}{d}\right)^{2}\right)\right]\frac{L}{d} \\ N_{r} &= \left[-\pi \left(\frac{d}{L}\right)^{2} K_{y}(0.03(C_{B}\frac{B}{d})^{2} - 0.15C_{B}\frac{B}{d} + 0.5)\right]\frac{L}{d} \\ N_{rrrr} &= \left[-0.0572 + 0.03C_{B}\frac{d}{L}\right]\frac{L}{d} \\ N_{rrrr} &= \left[-0.0572 + 0.03C_{B}\frac{d}{L}\right]\frac{L}{d} \\ N_{rrrr} &= \left[0.5d\frac{C_{B}}{B}\right] - 0.05 \\ N_{vrrr} &= \left[-0.0005 + 0.00594C_{B}\frac{d}{B}\right]\frac{L}{d} \end{split}$$

Lee et. al. (1998)

Yoshimura and Masumoto (2012) Kijima et. al. (1990)

Lee et. al. (1998)

Yoshimura and Masumoto (2012)	$N_{vrr} = -0.075(1 - C_B)\frac{L}{B} - 0.098$
Kijima et. al. (1990)	$N_{vvr} = -\left[57.5\left(C_B\frac{B}{L}\right)^2 - 18.4\left(C_B\frac{B}{L}\right) + 1.6\right]$
Lee et. al. (1998)	$N_{vvr} = \left[ -1.722 + 22.997 \left( C_B \frac{B}{L} \right) - 77.268 \left( C_B \frac{B}{L} \right)^2 \right] \frac{L}{d}$
Yoshimura and Masumoto (2012)	$N_{vvr} = \left[\frac{1.55C_B}{L/B} - 0.76\right]$

#### 3.3 Self-Propulsion Parameters

The empirical relations used to estimate wake fraction coefficient in straight motion  $(w_{P0})$  and thrust deduction factor  $(t_P)$  are given in Table 9 and Table 10, respectively. Empirical equations provided for self-propulsion parameters are based on the main particulars of ship and propeller such as L, B,  $C_B$  and  $D_P$ . Apart from these parameters, open water characteristics of the propeller  $(k_0, k_1, k_2)$  and the propeller revolution  $(n_P)$  must be known. Self-propulsion parameters given in MMG model can also be obtained by traditional engineering approach as explained in Kinaci et al. (2018).

<b>Table 9</b> . Empirical formulas for the wake fraction coefficient in straight motion, $w_{P0}$ .				
Reference	Empirical Formula			
Kijima et. al. (1990)	$w_{P0} = 0.5C_B - 0.05$			
Harvald (1983)	$w_{P0} = w_1 + w_2 + w_3$ $w_1 = a + \frac{b}{c(0.98 - C_B)^3 + 1}$ $w_2 = -\frac{0.05}{100(C_B - 0.7)^2 + 1}$ $w_3 = -0.18 + \frac{0.00756}{\frac{D_P}{L} + 0.002}$ $a = 0.1\frac{B}{L} + 0.149; \ b = 0.05\frac{B}{L} + 0.449; \ c = 585 - 5027\frac{B}{L} + 11700\left(\frac{B}{L}\right)^2$			
Tal	<b>Table 10</b> . Empirical formulas for the thrust deduction factor, $t_P$ .			
Reference	Empirical Formula			
Kulzyk (1995)	$t_P = -0.27$			
	$t_P = t_1 + t_2 + t_3$			
Harvald (1983)	$t_1 = d_1 + \frac{e_1}{f_1(0.98 - C_B)^3 + 1}$			

 $t_2 = 0.02$ 

$$t_{3} = 2\left(\frac{D_{P}}{L} - 0.04\right)$$
$$d_{1} = 0.625\frac{B}{L} + 0.08$$
$$e_{1} = 0.165 - \left(0.25\frac{B}{L}\right)$$
$$f_{1} = 525 - 8060\frac{B}{L} + 20300\left(\frac{B}{L}\right)^{2}$$

### 3.4 Rudder Parameters

The empirical relations embedded in MANSIM for estimation of hull-rudder interaction coefficients  $(t_R, a_H, x'_H)$  are given in Tables 11-13. Here,  $t_R$  is the deduction factor of rudder resistance due to the existence of ship hull,  $a_H$  denotes the factor of lateral force acting on the hull during steering and  $x'_H$  represents the application point of this lateral force component in longitudinal direction during steering. The empirical formulas for rudder force parameters are based on the main particulars of ship such as  $L, B, d, C_B$ . Alongside of hull-rudder interaction coefficients, there are some necessary coefficients ( $\varepsilon, \kappa, l'_R, \gamma$ ) to be known according to MMG model in order to predict rudder normal force ( $F_N$ ). The empirical relations for these coefficients given in literature are presented in Tables 14-17.

Reference	Empirical Formula	
Aoki et. al. (2006)	$a_H = 3.349 C_B^2 - 3.293 C_B + 1.059$	
Lee et. al. (1998)	$a_H = 2.78C_B - 1.922$	
Yoshimura and Masumoto (2012)	$a_H = 3.6C_B \frac{B}{L}$	
Quadvlieg (2013)	$a_H = 0.627C_B - 0.153$	
Lee and Shin (1998)	$a_{H} = -11.4036 + 40.94C_{B} - 81.11\frac{2d}{L} - 31.69C_{B}^{2} + 90.76\left(\frac{2d}{L}\right)^{2} + 79.47C_{B}\frac{2d}{L}$	

**Table 11**. Empirical formulations embedded in MANSIM for estimating  $a_H$ .

Reference	Empirical Formula	
Aoki et. al. (2006)	$x'_{H} = -0.45$	
Lee et. al. (1998)	$x'_H = 1.68C_B - 1.968 + 0.5$	
Yoshimura and Masumoto (2012)	$x'_H=-0.4$	

 $x'_{H} = -6.054 + 58.18\frac{B}{L} - 148.44\left(\frac{B}{L}\right)^{2}$ 

Lee and Shin (1998)

Reference	Empirical Formula	
Aoki et. al. (2006)	$t_R = -0.629 C_B^2 + 0.605 C_B + 0.129$	
Kijima (1990); Lee et. al. (1998)	$t_R = 0.45 - 0.28C_B$	
Yoshimura and Masumoto (2012)	$t_{R} = 0.39$	

**Table 13**. Empirical formulations embedded in MANSIM for estimating  $t_R$ .

<b>Table 14.</b> Empirical formulations embedded in MANSIM for estimating $\varepsilon$ .
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Reference	Empirical Formula
Kijima (1990)	$\varepsilon = -156.2 \left( C_B \frac{B}{L} \right)^2 + 41.6 \left( C_B \frac{B}{L} \right) - 1.76$
Lee and Shin (1998)	$\varepsilon = -2.3281 + 8.697C_B - 3.78\frac{2d}{L} + 1.19C_B^2 + 292\left(\frac{2d}{L}\right)^2 - 82.51C_B\frac{2d}{L}$
Yoshimura and Masumoto (2012)	$\varepsilon = 2.26 * 1.82(1 - w_{P0})$

# **Table 15**. Empirical formulations embedded in MANSIM for estimating $\kappa$ .

Reference	Empirical Formula
Lee and Shin (1998)	$\kappa = 0.6/(-2.3281 + 8.697C_B - 3.782d/L + 1.19C_B^2 + 292(2d/L)^2 - 82.51C_B2d/L)$
Yoshimura and Masumoto (2012)	$\kappa = 0.55/(2.26 * 1.82(1 - w_{P0}))$
Yoshimura and Ma (2003)	$\kappa = 0.55 - 0.8C_B B/L$

Table 16. Empirica	I formulations em	bedded in MANSIM	I for estimating $l'_R$ .
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· ·	- n	
Reference	Empirical Formula	
Kijima et. al. (1990)	$l_R' = 2x_R$	
Lee et. al. (1998)	$l_R' = 2x_R$	
Yoshimura and Masumoto (2012)	$l'_{R} = -0.9$	
Yoshimura and Ma (2003)	$l_R' = 1.7C_B \frac{B}{L} - 1.2$	

<b>Table 17</b> . Empirical formulations embedded in MANSIM for estimating $\gamma_R$ .
---

Reference	Empirical Formula
Kijima et. al. (1990)	$\gamma_R = -22.2 \left( C_B \frac{B}{L} \right)^2 + 0.02 \left( C_B \frac{B}{L} \right) + 0.68$

Lee et. al. (1998)	$\gamma_R = 2.7236C_B \frac{B}{L} + 0.021$
Yoshimura and Masumoto (2012)	$\gamma_R = 2.06C_B \frac{B}{L} + 0.14$
Lee and Shin	$\gamma_R^+ = 23.708 - 83.84C_B + 173.72\left(\frac{2d}{L}\right) + 71.64C_B^2 + 157\left(\frac{2d}{L}\right)^2 - 261.11C_B\left(\frac{2d}{L}\right)$
(1998)	$\gamma_R^- = 6.8736 - 16.77C_B + 3.5687\left(\frac{2d}{L}\right) + 4.68C_B^2 - 253.14\left(\frac{2d}{L}\right)^2 + 74.83C_B\left(\frac{2d}{L}\right)$

### 4 Graphical User Interface

The graphical user interface (GUI) of MANSIM provides a easy utilization to use mathematical models and empirical approaches, and has been designed to be a practical tool for ship maneuvering simulations. The mathematical models embedded in MANSIM are available for SPSR (Yasukawa and Yoshimura, 2015) and TPTR (Khanfir et al., 2011) ships to simulate the turning, zigzag and free maneuvers in calm water. Mathematical models for SPSR and TPTR ships were explained in detail in Section 2.2. Beside mathematical models, turning maneuver of single-propeller and twin-propeller ships can be predicted based on the empirical relations provided by Lyster and Knights (1979). The details of approach are given in Section 2.1. A flow diagramme of GUI of MANSIM is shown in Figure 2.



Figure 2. The workflow scheme of MANSIM.

The main solver code and functions of MANSIM were developed in MATLAB environment. The GUI was created with MATLAB Guide Layout editor which allows user to design different kinds of user interfaces with some basic tools (menus, toolbars, buttons, sliders, etc.). In the input section of MANSIM, the parameters required for mathematical model can be imported from a pre-prepared ".txt" file using the corresponding icon in toolbar instead of filling the text boxes one by one. Alternatively, if user has no input parameters except the main dimensions of ship, all inputs related to hull, propeller(s) and

rudder(s) can be calculated automatically by MANSIM using available empirical formulas embedded in software. The outputs obtained can be examined on user interface or can be exported as ".dat" file. It is also possible to visualize the trajectory of ships during turning/zigzag/free maneuvers as a 2D animation. Sample screenshots of input and output sections of MANSIM are shown in Figures 3-4. The pop-ups near some parameters in the input screen are used for the selection of empirical formulas embedded in the code. Note that the parameters of propeller and rudder in TPTR option have double values different from SPSR configuration, since TPTR ships may have different values for each parameters of rudder and propeller.

Maneuvering Ty	ype												
	(	Turning Maneuve	r			⊖ Zig	zag Mane	uver					
Main Dimensior	IS		Hydrodynai	nic D	erivatives								
L=	320	m	× o	-	-0.022 ·	~	Υ <sub>V</sub> =	-0.315	~	N	= -0.13	7	$\sim$
B=	58	m	x <sub>vv</sub>	-	-0.04 ·	~	Y <sub>VV</sub> =	-1.607	🗸	N	-0.03		$\sim$
d=	20.8	m	x <sub>vvvv</sub>	=	0.771 ·	~	Υ <sub>Γ</sub> =	0.083	~	N	= -0.04	9	$\sim$
C <sub>B</sub> =	0.81	-	x <sub>rr</sub>	-	0.011	~	Y <sub>rrr</sub> =	0.008	~	N rrr	-0.01	3	$\sim$
LCG=	0.035	-	x <sub>vr</sub>	-	0.002 .	~	Y <sub>vrr</sub> =	-0.391		N vrr	= 0.05	5	$\sim$
							Y <sub>vvr</sub> =	0.379	~	N vvr	= -0.29	4	$\sim$
Hydrodynamic	Properties	5	Propeller P	aram	eters								
ρ =	1025	kg/m <sup>3</sup>		D=	9.86	m		w	-	0.35	×		
m <sub>x</sub> =	0.022	v		n=	1.53	rps		k <sub>0</sub>	=	0.2931	-		
m _=	0.223	×	t	p =	0.22	-	×	k 1	-	0.2753	-		
J <sub>z</sub> =	0.011	~	×	р <sup>=</sup>	-0.48	•		k 2		0.1385	-		
Inital Values			-Rudder Par	amet	ers								
r				H=	15.8	m		×	_	-0.5	-		
U =	7.9732	m/s	a	н=	0.312	٦.	~	ĩ	_	-0.71	~	1	
δ =	35	deg	×	=	-0.464	-	~	۱ ک	۲ =	1.827	-		
			t	R R	0.387	-	~	A	-	112.5	m²		
Solver Paramet	ers		:	ε =	1.09	-	~	γ+	-	0.64	~		
T =	1610	S	•	c =	0.5	-	~	γ-	-	0.395	~		
t=	0	S			RE	SET							
<u>Δ</u> T=	0.1	S			MAIN	I MENU				RUN			

Figure 3. Sample screenshot of the input section of 3DOF-MMG approach in MANSIM.



Figure 4. Sample screenshot of the output section of turning/zigzag maneuver in MANSIM.

# 5 Application of MANSIM to Benchmark Ships

In this section, turning and zigzag maneuvers computed by MANSIM were validated for two benchmark ships, namely, KVLCC2 and DTMB5415 hulls. KVLCC2 tanker is a SPSR ship, while DTMB5415 has a TPTR configuration. The mathematical models for these type of ships are available in MANSIM and described in section 2.2. Available experimental and computational results for hydrodynamic derivatives, rudder force and self-propulsion parameters were used to compare the turning and zigzag maneuvers for both ships. Hydrodynamic derivatives obtained numerically have free surface effects taken into account since both ships have relatively high Froude numbers (Kinaci et al., 2016). Simulation results were compared with free running data available in literature. Furthermore, influence of variation of hydrodynamic derivatives and rudder parameters on maneuvering indices such as advance, tactical diameter, overshoot angles, etc. were investigated systematically by performing a comprehensive sensitivity analysis.

# 5.1 Simulation of Turning and Zigzag Maneuvers of KVLCC2

Turning and zigzag maneuvers of full-scale KVLCC2 tanker have been simulated by MANSIM using the hydrodynamic derivatives, rudder and propeller parameters given in Yasukawa and Yoshimura (2015) who have conducted circular motion and rudder force tests for the 1/110 scaled model of KVLCC2. Free running results are also available for this ship and these tests have been carried out by MARIN for the 1/45.7 scaled model (ftp://ftp.forcetechnology.com). The maneuvering results of  $35^{\circ}$  and  $-35^{\circ}$  turning circle, and 10/10, -10/-10, 20/20, -20/-20 zigzag maneuvers predicted by MANSIM were compared with those of free running tests for full-scale KVLCC2. Input parameters of MANSIM for the prediction of maneuvering performance are given in Table 18. Comparison of results for port and starboard turnings are shown in Figures 5 and 6. Note that both results are in good agreement.

$L_{pp}(m)$	320	B(m)	58	d(m)	20.8	$C_B$	0.81			
			Hydrodyna	mic Derivativ	es					
$X'_0$	0.022	$m'_x$	0.022	$Y'_{vrr}$	-0.391	$N'_r$	-0.049			
$X'_{\nu\nu}$	-0.040	$Y'_{v}$	-0.315	$Y'_{vvr}$	0.379	$N'_{rrr}$	-0.013			
$X'_{\nu\nu\nu\nu}$	0.771	$Y'_{vvv}$	-1.607	$m'_y$	0.223	$N'_{vrr}$	0.055			
$X'_{rr}$	0.011	$Y'_r$	0.083	$N'_{v}$	-0.137	$N'_{vvr}$	-0.294			
$X'_{vr}$	0.002	$Y'_{rrr}$	0.008	$N'_{\nu\nu\nu}$	-0.030	$J'_z$	0.011			
		(	Components	of Propeller F	orce					
$D_P(m)$	9.86	$t_P$	0.22	<i>k</i> <sub>1</sub>	-0.275	$k_0$	0.293			
$n_P(rps)$	1.53	$W_{P0}$	0.35	$k_2$	-0.139	$x_P$	-0.48			
		Compo	nents of Rud	der Forces ar	nd Moment					
$H_R(m)$	15.8	λ	1.827	$x'_H$	-0.464	$l'_R$	-0.71			
$x'_R$	-0.50	$a_H$	0.312	ε	1.09	$\gamma_R~(\beta_R < 0)$	0.395			
$A_R(m^2)$	112.5	$t_R$	0.387	κ	0.50	$\gamma_R~(eta_R>0)$	0.64			

**Table 18**. The inputs of MANSIM for the prediction of maneuvering abilities of full-scale KVLCC2.

The turning maneuver indices such as advance (Ad), transfer (Tr), tactical diameter (TD), steady turning diameter (STD), steady yaw rate (SYR), steady turning speed (STS) and steady drift angle (SDA) were obtained for the full-scale KVLCC2 tanker and shown in Table 19. It can be said that the results calculated by MANSIM agree well with the free running data. The history of kinematical parameters were underpredicted slightly except steady yaw rate that has a perfect match. The largest difference is around 20% in speed reduction. However, this discrepancy can also be attributed to the differences in propeller rotation rate. The calculations are based on the self-propulsion point of the full scale ship whereas the free running tests are conducted by the self-propulsion point of model ship. This is most likely the primary reason of differences in the turning circle trajectories. It can be also stated that the results of empirical approach seem to be in accordance when compared with experiments.





Figure 5. Comparison of  $-35^{\circ}$  turning maneuver results of KVLCC2 by MANSIM with free running (FR) data (Fr = 0.142).

		$\delta = \cdot$	-35°		$\delta = 35^{\circ}$			
Maneuvering	MARIN	MANSIM	Yasukawa	Lyster	MARIN	MANSIM	Yasukawa	Lyster
Indices	FR	SB	SB	EMP	FR	SB	SB	EMP
			(2015)	(1979)			(2015)	(1979)
Ad (-)	3.11	3.10	3.56	2.76	3.25	3.10	3.67	2.76
Tr (-)	-1.22	-1.23	-1.51	-1.30	1.36	1.35	1.58	1.30
TD (-)	-3.08	-2.90	-3.59	-2.75	3.34	3.16	3.71	2.75
STD (-)	2.48	2.05	-	2.06	2.54	2.31	-	2.06
SYR (-)	-0.30	-0.30	-	-	0.29	0.28	-	-
STS (-)	0.36	0.29	-	0.35	0.38	0.32	-	0.35
SDA (deg)	-19.83	-21.51	-	-	18.59	20.24	-	-

**Table 19**. Comparison of turning maneuver indices of full-scale KVLCC2.





Figure 6. Comparison of 35° turning maneuver results of KVLCC2 by MANSIM with free running (FR) data (Fr = 0.142).

Comparison of various type of predicted zigzag maneuvers with free running data for full-scale KVLCC2 is shown in Figures 7-10. Agreement in the first overshoot angles (OA) are better than the second overshoot angles for both -10/-10 and 10/10 zigzag maneuvers. OAs in -20/-20 and 20/20 zigzag maneuvers are shown in Figures 9-10 and general trend of zigzag motion agree well with the free running data. It can also be deduced from these figures that the phase shifts in trajectories are generally caused by the mismatch in rudder execution times.

Maneuvering indices of zigzag motion are considered as  $1^{st}$  and  $2^{nd}$  OAs for -10/-10, 10/10, -20/-20 and 20/20 maneuvers, and comparison of results are given in Table 20. Scale effect could be a reason for these discrepancies since the hydrodynamic derivatives and other parameters have been obtained at model scale of ship. Furthermore, a more precise prediction method may be required to improve the accuracy of results instead of using empirical approaches for the terms of added mass and added moment of inertia. It should be also noted that the accuracy of prediction was found to be strongly related with the initial conditions (approach speed, rudder angle, propeller rate, etc.) in zigzag maneuvers.

Maneuver	OAs (deg)	MARIN-FR	MANSIM-SB	Yasukawa-SB
				(2015)
-10/-10	$1^{st}$	9.5	7.5	8.8
	$2^{nd}$	15	9.4	12.6
10/10	$1^{st}$	8.2	5.3	5.8
10/10	$2^{nd}$	21.9	14.1	20.5
20/ 20	$1^{st}$	15.1	14.2	16.1
-20/-20	$2^{nd}$	13.3	11.8	14.6
20/20	$1^{st}$	13.7	11.1	11.8
20/20	$2^{nd}$	14.9	15.5	19.7

<b>Table 20</b> . C	omparison o	of the p	redicted	maneuv	ering ir	ndices	of full-so	ale KV:	LCC2	with t	he free
			running	data in	zigzag r	motion	IS.				



**Figure 7**. Comparison of the predicted heading angle, rudder angle and trajectory with free running (FR) data in -10/-10 zigzag maneuver (Fr = 0.142).



**Figure 8**. Comparison of the predicted heading angle, rudder angle and trajectory with free running (FR) data in 10/10 zigzag maneuver (Fr = 0.142).



Figure 9. Comparison of the predicted heading angle, rudder angle and trajectory with free running (FR) data in -20/-20 zigzag maneuver (Fr = 0.142).



Figure 10. Comparison of the predicted heading angle, rudder angle and trajectory with free running (FR) data in 20/20 zigzag maneuver (Fr = 0.142).

### 5.2 Simulation of Turning and Zigzag Maneuvers of DTMB5415

Subsequent to maneuvering simulation of KVLCC2, a system-based simulation was also performed for full-scale DTMB5415 surface combatant by using MANSIM to predict its turning and zigzag maneuverabilities. Hydrodynamic derivatives and other parameters related to the propeller and rudder were computed by CFD for the 1/46.588 scaled model of DTMB5415 hull (Sukas et al., 2019). Since DTMB5415 has a TPTR configuration, propeller and rudder parameters may show difference due to asymmetric flow around the control surfaces during maneuvering motion. For validation, system based (SB) simulation results of 35 and -35 turning maneuvers, and -20/20 zigzag manuever were compared with those of free running tests carried out by MARIN (<u>ftp://ftp.forcetechnology.com</u>). The input parameters of MANSIM for full-scale DTMB5415 hull are given in Table 21. The parameters with superscripts "S" and "P" indicate the values for starboard and port sides, respectively. The predicted results of trajectory, yaw rate and speed loss were compared with experimental data for -35 and 35 turning maneuvers and shown in Figures 11-12.

Main Particulars of DTMB5415											
$L_{pp}(m)$	142	B(m)	19.06	d(m)	6.15	$C_B$	0.507				
	Hydrodynamic Derivatives										
$X'_0$	0.016	$Y'_{v}$	-0.294	$Y'_{vvr}$	-1.506	$N'_{rrr}$	-0.048				
$X'_{vv}$	-0.182	$Y'_{\nu\nu\nu}$	-1.174	$m_y'$	0.108	$N'_{vrr}$	-0.218				
$X'_{rr}$	-0.028	$Y'_r$	-0.047	$N'_{v}$	-0.162	$N'_{vvr}$	-0.800				
$X'_{vr}$	-0.093	$Y'_{rrr}$	-0.052	$N'_{vvv}$	-0.225	$J'_z$	0.008				
$m'_x$	0.007	$Y'_{vrr}$	-0.784	$N_r'$	-0.045						
		Com	ponents of I	Propeller F	orce and Mo	ment					
$D_P^{P,S}(m)$	6.15	$t_P^{P,S}$	0.210	$k_0^{P,S}$	0.398	$k_1^{P,S}$	-0.299				
$n_P^{P,S}(rps)$	1.65	$W_{P0}^{P,S}$	0.073	$k_2^{P,S}$	-0.141	$x_{P}^{\prime P,S},  y_{P}^{\prime P,S} $	-0.462, 0.244				

Components of Rudders Force and Moment										
$H_R^{P,S}(m)$	4.38	$a_{H}^{P,S}$	0.086	$\varepsilon^{P,S}$	0.93;1.00	$x_{R}^{\prime P,S}$ , $ y_{R}^{\prime P,S} $	-0.472, 0.267			
$\lambda^{P,S}$	1.26	$t_R^{P,S}$	0.440	$\kappa^{P,S}$	0.62;0.70	$\gamma_R^{P,S}~(\beta_R < 0)$	0.53;0.37			

-0.944

0.37;0.53

-0.437

 $\lambda^{P,S}$ 

 $A_R^{P,S}(m^2)$ 

15.4



Figure 11. Comparison of  $-35^{\circ}$  turning maneuver results of DTMB5415 by MANSIM with free running (FR) data (Fr = 0.25).



Figure 12. Comparison of  $35^{\circ}$  turning maneuver results of DTMB5415 by MANSIM with free running (FR) data (Fr = 0.25).

According to the results shown in Figures 12-13, free running data seems to have larger difference in port and starboard turnings than those of MANSIM. This discrepancy in experiments can be explained with the asymmetry between the values of rudder parameters for port and starboard turnings. On the other hand, there is a large relative error between MANSIM and free running data in starboard turning for DTMB5415 and it is most likely due to the symmetry assumption for the rudder and propeller parameters in CFD analyses. Because all necessary rudder and propeller parameters of DTMB5415 were estimated by CFD [3] for port turning and it was assumed that these parameters are identical/symmetrical with the starboard turning. Another reason for the discrepancies in Figures 12-13 may be caused from neglecting the roll-coupled effects for DTMB5415. The yaw rate of ship was slightly overestimated by MANSIM which leads to a smaller turning trajectory prediction. The percentages of speed reduction during maneuver were estimated higher than the free running results for both side turnings. The turning maneuver indices of full-scale DTMB5415 are given in Table 22. The results obtained by empirical approach also seem to be underpredicted as compared to the experiments.

		$\delta = \cdot$	–35°		$\delta = 35^{\circ}$					
Maneuvering	MARIN	MANSIM	Carrica	Lyster	MARIN	MANSIM	Carrica	Lyster		
Indices	FR	SB	CFDB	EMP	FR	SB	CFDB	EMP		
			(2013)	(1979)			(2013)	(1979)		
Ad (-)	2.71	2.59	2.90	2.55	3.19	2.40	2.90	2.55		
Tr (-)	-1.46	-1.35	-1.58	-1.15	1.33	1.17	1.58	1.15		
TD (-)	-3.65	-3.48	-3.87	-2.83	3.60	3.14	3.87	2.83		
STD (-)	3.66	3.53	-	2.69	3.75	3.19	-	2.69		
SYR (-)	-0.38	-0.41	-	-	0.39	0.43	-	-		
STS (-)	0.75	0.72	-	0.62	0.74	0.68	-	0.62		

Table 22. Comparison of turning maneuver indices of full-scale DTMB5415.

Predicted heading/rudder angles and trajectory for -20/-20 zigzag maneuver were also compared with free running data and shown in Figure 13. Despite a good agreement of the predicted overshoot angles with the experiments, there is a discrepancy in trajectories due to the early execution time of second and third deflections of rudder in the system-based simulation. Maneuvering indices of zigzag motion were compared in terms of  $1^{st}$  and  $2^{nd}$  OAs and given in Table 23. As it was mentioned previously, accuracy of results can be influenced by slight differences with the experimental procedure such as initial conditions of the model. It can be also noted that the results by MANSIM are based on the self-propulsion point of the full scale ship whereas the free running tests are conducted by the selfpropulsion point of model ship. This can be stated as an another reason for differences in the turning and zigzag trajectories of DTMB5415.



**Figure 13**. Comparison of the predicted heading angle, rudder angle and trajectory of full-scale DTMB5415 with free running (FR) data in -20/-20 zigzag maneuver (Fr = 0.25).

Table 23. Comparison of the predicted maneuvering indices of full-scale DTMB5415 with the free
running data in $-20/-20$ zigzag maneuver.

Maneuver	OAs (deg)	MARIN-FR	MANSIM-SB	Carrica-CFDB
-20/-20	$1^{st}$	4.70	5.12	7.30
	$2^{nd}$	4.80	6.34	7.20

#### 5.3 Sensitivity Analysis of Hydrodynamic Derivatives and Rudder Parameters

Standard MMG model used in MANSIM consists of a total of 17 hydrodynamic derivatives in the maneuvering equations of motion. In addition, propeller and rudder parameters are included into these equations to simulate free running tests. Utilizing the user interface of MANSIM, parametrical studies such as sensitivity analysis can be performed readily and effect of any parameter on general maneuvering performance of ships can be investigated in detail. Here, a sensitivity analysis was performed for KVLCC2 and DTMB5415 ships to investigate the effect of each hydrodynamic derivative and rudder parameters on the turning and zigzag maneuverabilities.  $-35^{\circ}$  turning and  $-20^{\circ}/-20^{\circ}$  zigzag maneuvers were selected as sample cases to be examined, and the influence of variation of hydrodynamic derivatives/rudder parameters on maneuvering indices such as advance (Ad), transfer (Tr), tactical diameter (TD), steady turning diameter (STD) and overshoot angles (OA) were investigated. The original value of parameters was increased seperately by 25% and used in the mathematical model. The sensitivity analysis was carried out using the index proposed by Sen (2000) and it was adopted to examine the variation of maneuvering indices caused by changes in each hydrodynamic derivative and rudder parameter. The sensitivity index *S* is represented as given in Eqn. 21:

$$S = \frac{(R - R^*)/R^*}{(H - H^*)/H^*}$$
(21)

where,  $R^*$  and  $H^*$  denote the original values of maneuvering index and corresponding hydrodynamic derivative/rudder parameter, respectively. R and H represent the increased values by 25%. After calculating S, all these values of parameters are summed up and a total value for each indice is obtained. Then, sensitivity index for each parameter is divided by the total value of this indice. For example, percentage of the effect of  $X'_0$  in advance is calculated by,

$$\% S_{X_0',Ad} = 100 \cdot \frac{S_{X_0'}}{S_{Ad}}$$
(22)

Here;  $\% S_{X'_0,Ad}$  denotes the effect of  $X'_0$  in percentages,  $S_{X'_0}$  is the sensitivity index of  $X'_0$  and  $S_{Ad}$  is the total sensitivity index value for advance index. Sensitivity of each parameter as a percentage for each maneuvering index for KVLCC2 and DTMB5415 are given in Tables 24 and 25. In these tables, parameters which have greater value than or at least equal to 10% were considered to be highly effective as shown in bold. Parameters, which are between in the range of 3% - 10%, were considered to have mediocre at best as shown in underlined.

Daramators		Turning Man	Zigzag Mane	Zigzag Maneuver Indices			
Parameters —	Ad	Tr	TD	STD	1 <sup>st</sup> 0A	2 <sup>nd</sup> 0A	
$X'_0$	2.74	2.94	<u>3.17</u>	1.68	0.88	<u>3.99</u>	
$X'_{\nu\nu}$	0.46	0.00	0.32	0.42	0.35	0.20	
$X'_{\nu\nu\nu\nu}$	0.46	0.00	0.32	0.84	0.35	0.40	
$X'_{rr}$	0.46	0.00	0.32	0.84	0.35	0.40	
$X'_{vr}$	0.46	0.00	0.00	0.00	0.35	0.20	
$Y'_{\nu}$	0.00	<u>5.88</u>	2.54	0.84	<u>8.13</u>	<u>5.59</u>	
$Y'_{\nu\nu\nu}$	0.46	0.88	0.00	0.42	0.18	1.00	
$Y'_r$	0.46	<u>3.82</u>	2.22	0.42	<u>5.30</u>	2.59	
$Y'_{rrr}$	0.46	0.00	0.00	0.00	0.35	0.20	
$Y'_{vrr}$	0.46	2.06	0.32	0.42	0.53	0.80	

 Table 24. Sensitivity analysis of hydrodynamic derivatives and rudder parameters of KVLCC2 in turning and zigzag maneuvers.

$Y'_{vvr}$	0.46	0.88	0.00	0.00	0.18	0.40
$N_{\nu}'$	14.16	13.53	13.02	<u>6.95</u>	34.45	29.14
$N'_{vvv}$	0.46	0.00	0.32	0.00	0.53	0.40
$N_r'$	15.53	12.35	12.38	<u>8.21</u>	15.02	13.97
$N'_{rrr}$	0.46	0.88	1.27	2.11	0.00	0.40
$N'_{vrr}$	1.37	2.06	2.54	2.95	0.18	1.00
$N'_{vvr}$	2.74	<u>4.71</u>	<u>6.98</u>	<u>6.53</u>	1.41	<u>3.59</u>
$m'_x$	0.46	0.88	0.00	0.42	2.30	1.20
$m'_y$	0.46	0.00	2.22	4.84	1.94	0.20
$J'_z$	1.83	0.00	0.32	0.00	<u>3.36</u>	<u>4.39</u>
$a_H$	<u>4.11</u>	2.94	2.54	2.53	1.41	2.79
$x'_H$	<u>3.65</u>	2.06	2.22	2.53	1.77	2.40
$t_R$	0.00	0.88	0.95	2.11	0.53	0.80
Е	31.96	26.76	27.30	28.00	<u>6.01</u>	10.18
κ	11.42	<u>9.71</u>	11.75	19.79	<u>3.71</u>	<u>6.59</u>
$\gamma_R$	2.74	<u>3.82</u>	4.44	<u>4.21</u>	<u>6.71</u>	0.80
$l'_R$	1.83	2.94	2.54	2.95	<u>3.71</u>	<u>6.39</u>

According to Table 24, hydrodynamic derivatives related to surge force X have lower effect than that of the sway force and yaw moment derivatives, on the results. Only the resistance coefficient  $X'_0$  has a moderate effect on transfer, tactical diameter and second overshoot angles. First order derivatives seem to have a strong influence on maneuvers especially on zigzag indices, where  $N'_v$  has the highest impact among all. High order and coupled derivatives have lower effect on maneuvering indices except  $N'_{vvr}$ . The terms of added mass and added moment of inertia have a moderate effect on first overshoot angle, while only  $m'_y$  has a moderate effect on steady turning radius. Rudder parameters have also major influence on maneuvering indices. Particularly, variation of  $\varepsilon$  and  $\kappa$  greatly affects the turning and zigzag maneuvers of ship. It can briefly be stated for the sensitivity analysis of KVLCC2 tanker that the overshoot angles are more sensitive to the variations of hydrodynamic derivatives and rudder parameters than those of turning maneuver. In addition, advance distance and steady turning diameter seem to be the least and most influenced indices by the variation of parameters in turning maneuver.

Devene atova		Turning Man	euver Indices	Zigzag Mane	Zigzag Maneuver Indices			
Parameters —	Ad	Tr	TD	STD	$1^{st} OA$	$2^{nd} OA$		
$X'_0$	0.82	0.00	0.00	0.00	2.15	2.85		
$X'_{\nu\nu}$	0.00	0.00	0.00	0.00	0.66	0.67		
$X'_{rr}$	0.00	0.00	0.00	0.00	0.83	0.67		
$X'_{vr}$	0.00	0.00	0.00	0.00	0.83	1.34		
$Y'_{\nu}$	2.45	<u>4.16</u>	0.00	0.71	2.48	1.68		
$Y'_{\nu\nu\nu}$	0.82	0.83	0.00	0.36	0.33	0.84		
$Y'_r$	0.82	1.66	0.35	0.36	1.49	0.50		
$Y'_{rrr}$	0.00	0.00	0.00	0.00	0.33	0.50		
$Y'_{vrr}$	2.45	2.49	0.35	0.71	0.66	0.50		
$Y'_{vvr}$	<u>3.27</u>	1.66	1.75	1.79	1.49	0.67		
$N'_{v}$	13.88	10.80	14.39	14.29	17.36	15.10		
$N'_{\nu\nu\nu}$	1.22	0.83	1.05	1.07	0.83	0.17		
$N'_r$	11.84	<u>9.14</u>	10.88	11.07	<u>8.60</u>	<u>7.55</u>		
$N'_{rrr}$	<u>3.27</u>	<u>3.32</u>	<u>3.51</u>	<u>3.57</u>	0.50	2.01		
$N'_{vrr}$	<u>6.94</u>	<u>5.82</u>	<u>7.72</u>	<u>7.14</u>	2.98	<u>3.52</u>		

 Table 25. Sensitivity analysis of hydrodynamic derivatives and rudder parameters of DTMB5415 in turning and zigzag maneuvers.

$N'_{vvr}$	<u>9.39</u>	<u>9.97</u>	12.63	12.14	<u>3.31</u>	<u>4.70</u>
$m'_x$	0.00	0.00	0.00	0.00	0.83	0.67
$m'_y$	0.00	0.83	0.35	0.00	1.49	0.67
$J'_z$	1.22	0.00	0.00	0.00	<u>4.13</u>	<u>3.02</u>
$a_H$	0.82	0.00	0.35	0.00	0.00	1.17
$x'_H$	0.00	0.83	0.35	0.36	0.33	0.50
$t_R$	<u>3.27</u>	2.49	<u>3.16</u>	<u>3.21</u>	0.17	0.50
ε	10.20	0.00	2.46	2.50	16.03	18.29
κ	0.82	0.83	0.00	0.36	<u>3.14</u>	<u>6.21</u>
$\gamma_R$	15.92	26.32	24.21	23.93	17.02	15.27
$l'_R$	10.61	18.01	16.49	16.43	12.07	10.40

Table 25 shows the sensitivity indices of turning and zigzag maneuver of DTMB5415 hull. Note that the parameters of port and starboard rudders of DTMB5415 are increased together. Similar to KVLCC2 hull,  $N'_{v}$  was found to be the most dominant linear derivative in both turning and zigzag maneuvers of DTMB5415 hull. The nonlinear derivatives have small effects except  $N'_{rrr}$  which affects the manuevers moderately. The coupled derivatives related to the yaw moment  $(N'_{vvr}, N'_{vrr})$  have relatively major impact as compared to those of surge and sway forces.  $X'_{vv}$ ,  $X'_{rr}$ ,  $X'_{vr}$ ,  $Y'_{rrr}$  and  $m'_{x}$  have almost no influence on the indices of turning maneuver. Rudder parameters have a significant effect on the maneuvers rather than the hydrodynamic derivatives. Additionally, similar to KVLCC2 case, advance distance was found to be the least influenced index from the variation of hydrodynamic derivatives and rudder parameters. On the whole, it can be noted for both ships that the derivatives based on yaw moment are very influential on turning and zigzag maneuvers. The indices of zigzag motion are oversensitive to the variation of parameters in MMG model. The terms of added mass and added moment of inertia have relatively low effect than the other parameters especially in turning motion so that they are generally estimated based on empirical formulas or charts. Results of sensitivity analysis for both ships are summarized in Table 26.

	Turning Maneuver				Zigzag Maneuver			
	KVLCC2		DTMB5415		KVLCC2		DTMB5415	
Impact Level	High	Mediocre	High	Mediocre	High	Mediocre	High	Mediocre
Hydrodynamic derivatives	$N'_{v}, N'_{r}$	N'vvr	$N'_{v}, N'_{r}, N'_{vvr}$	Y', Y' <sub>vvr</sub> , N' <sub>rrr</sub> , N' <sub>vrr</sub>	$N'_v, N'_r$	$Y'_v, Y'_r, J'_z$	$N_{v}^{\prime}$	$N'_r, N'_{vvr}, N'_{vrr}, J'_z$
Rudder parameters	ε, κ	$\gamma_R$	$\varepsilon, \gamma_R, l'_R$	$t_R$	ε	$\kappa, \gamma_R, l'_R$	$\varepsilon, \gamma_R, l'_R$	κ

Table 26. Parameters that have high or mediocre impact for turning circle and zigzag maneuvers.

### 6 Conclusions

In this study, a user-friendly ship maneuvering code based on MMG mathematical model has been introduced. The graphical user interface of code allows to make an easy and simple changes to hydrodynamic derivatives or propeller/rudder parameters. The software provides a basis for researchers to play with all the coefficients / parameters and to have a better understanding of ship maneuvering phenomena which involves a dynamic and complex background. It also contains many empirical relations suggested by many researchers in the field of ship maneuvering. The software is considered to be helpful especially for sensitivity analysis on maneuvering. A SPSR and a TPTR ship

have been investigated and parameters that have significant effect on each maneuvering indice have been found. Findings can be listed as follows:

- $N_v$  and  $N_r$  are highly effective on hydrodynamic coefficients in ship maneuvering.
- $\varepsilon$  is a highly effective rudder parameter in ship maneuvering.
- Coupled terms have a non-negligible importance for DTMB5415 ship.
- Rudder parameters have higher importance in zigzag motion of DTMB5415 ship.

Although the last two statements are only applicable for DTMB5415 ship, it is considered that they are valid for TPTR ships in general. However, more research is needed to solidify these statements.

Currently, MANSIM does not take into account the external disturbances. Effects of wind, wave and current are also to be included into the software. Another study is to add a quadratic model to the code, which is only working with cubic model in its current form. Furthermore, 3-DOF MMG model will be expanded to a 4-DOF model which includes the roll-coupled effects.

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